

Comparing retrieved optical depth from a high-order model and a zero-order model and analyzing their relationship with vegetation properties

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Abstract

Optical depth is significant key vegetation parameters in the study of vegetation canopy. Until now efforts have been made to estimate optical depth by fitting sensors brightness temperature to a zero-order model (τ - ω model). The τ - ω model is a simple model without considering multi-scattering effects inside the vegetation layer. Here effective optical depth (VODs) calculated from a high order model to take in to account multi-scattering effects. The high order model is a close simulation of the real situation. It enables investigating optical depth behavior during wheat grow season in different frequencies, incident angels and polarizations. Measured LAI, VWC and biomass were used to validate simulated VODs. VODs was corresponding to the measured vegetation parameters in terms of the trend and the time of maximum and the minimum values. Furthermore, equivalent optical depth (EVOD) was calculated by fitting brightness temperature to the zero-order model and compared with the VODs. Results indicated EVOD as VODs also were frequency, incident angle and polarization dependent but overestimated compare to VODs. Calculating optical depth of other types of vegetation with different structure can give more detailed in vegetation behavior during growing season.

1. Introduction

Vegetation, as a significant aspect of the ecosystem, has been widely studied in terms of monitoring its properties such as biomass, water content and coverage. Optical depth is significant key parameter in the study of vegetation canopy (Baur et al. 2019). Microwave attenuation properties of vegetation canopy can be explained by optical depth. Temporal optical depth is an effective parameter in monitoring biomass, VWC, crop water stress, global change monitoring, vegetation phenology, and drought (Jones et al. 2011; Liu et al. 2011; Guan et al. 2013; Guan et al. 2014; Ulaby et al. 2014). Radiative transfer models (RTM) are common to calculate optical depth and scattering albedo (Shi et al. 2008). High order models and zero order models are two types of RTM models. A high order model is a close simulation of the real situation by considering multi scattering effects insides the vegetation that enabled us to investigate optical depth and scattering albedo behavior in different frequencies, incident angels and polarizations during the vegetation growing season. The zero-order model (τ - ω model) is a simple radiative transfer model that simulates brightness temperature as a function of optical depth, single scattering albedo and soil emissivity. This model doesn't consider multi-scattering effects in the vegetation layer (Ferrazzoli et al. 2002). Nowadays in the microwave region of electromagnetic spectrum, the τ - ω inverse model from soil and vegetation layers is widely used to calculate soil moisture and optical depth for when scattering albedo was either eliminated or had a constant value (Jackson, 1993; Owe et al. 2001; Kerr et al. 2012; O'Neill et al. 2018; Gao et al. 2020). Techniques like the Single Channel Algorithm (SCA) (Jackson, 1993), The Dual Channel Algorithm (DCA) (O'Neill et al., 2018), Land Parameter Retrieval Model (LPRM) (Owe et al., 2001; De Jeu and Owe, 2003), Multi-Temporal Dual Channel Algorithm (MT-DCA), Multi-angular algorithm (SMOS standard algorithm) (Kerr et al. 2012; Al Bitar et al. 2017), Constrained Multi-Channel Algorithm (CMCA) (Ebtehaj and Bras, 2019;

Gao et al., 2020; Konings et al., 2016), Multi-Channel Collaborative Algorithm (MCCA) (Zhao et al., 2021) were used to calculate effective optical depth and soil moisture from the τ - ω inverse model.

Accordingly, the main goals of this study are:

- Calculating effective (theoretical) optical depth, by the high order model (Tor Vergata University model) and validating the results with measured parameters (LAI, VWC and biomass) during wheat growing season.
- Calculating effective (Equivalent) optical depth using fitting method by a way these two parameters were polarization, incident angle, and frequency dependent during wheat planting to harvesting.
- Comparing the effective results with equivalent values to understand whether fitting method retrievals changes are the same as physical method retrieval changes or not.

2. Materials and Methods

2.1 Study area

Wheat canopy data were obtained at the Institute National de Recherches Agronomiques (INRA) test site in summer 1993. Measurements get from Day of Year (DOY) 90 (shortly after seeding) to DOY 175 (before harvest). They were recorded for leaf length, leaf width and thickness, stalk diameter and length; canopy height; stalk length; stalk and leaf moisture; soil and plant temperature; leaf inclination angle; density; and volumetric soil moisture (SMC). Leaf Area Index (LAI), fresh and dry biomass and VWC also were recorded. Detailed and more field data information is in Ferrazzoli et al. (Ferrazzoli et al. 2000). Multi-Frequency Microwave Radiometer (PORTOS) was used to measure the passive microwave signal or brightness temperature (TB) of wheat. It has six different frequency antennae with dual-polarized (V/H) observations. The calm water surfaces were used to do regular calibration with radiometer absolute accuracy in 3 K. Table 1 showed input variables to the models.

	Wheat Parameter	Unit	Min.	Max.
Leaf	Radius	cm	0.2	0.56
	Thickness	mm	0.017	0.02
	Gravimetric Moisture	%	0.66	0.81
	Angle Distribution	degree	5	85
	Radius	cm	0.108	0.22
Stalk	Length	cm	3.57	76.3
	Gravimetric Moisture	%	0.66	0.84
	Angle Distribution	degree	0	0
	Mean Stalk Density	m ²	80	600
Layer	Layer Height	m	0.16	99

Table 1. Wheat input data for the Tor Vergata model

2.2 Optical depth by Tor Vergata University model

Optical depth for vegetation is used to describe attenuation properties, in fact, it is a measure of how opaque a vegetation canopy is when radiation passing through it (De Jeu et al. 2009). It is important in estimating soil moisture and can provide unique information on vegetation biomass and water content and canopy structure retrieval (Ulaby et al. 1982).

By means of forward scattering theorem, in vegetation transmissivity ($\lambda_p(\theta) = e^{-\tau_p \sec \theta}$) function, τ is vegetation opacity and is given by ($\tau_p(\theta) = k_{ep}(\theta)d$) where θ is observation angle from the nadir and d is canopy layer height and k_{ep} is the average vegetation extinction coefficient (Kurum et al. 2011). The effective optical calculated from the Tor Vergata University model by taking in to account multi scattering effects which were named VODs.

2.3 Equivalent optical depth by fitted τ - ω model

The rough surface models make the relationship between radiometer data and some properties of the observed surface such as soil moisture and vegetation optical depth. A simple zero-order model as the τ - ω model is useful and can obtain the observed surface properties by the simple process and straightforward (Kurum et al. 2011).

$$T_{B_{p,f}} = [(1 - \omega_{p,f,v})(1 - \gamma_{p,f,v})(1 - e_{p,f}^{surf})(1 + \gamma_{p,f,v})]T^{veg} + (\gamma_{p,f,v}T^{soil} - [(1 - \omega_{p,f,v})(1 - \gamma_{p,f,v})(1 - e_{p,f}^{surf})\gamma_{p,f,v}]T^{veg})e_{p,f}^{surf}$$

Equivalent scattering albedo and optical depth from a non-scattering medium with the same emissivity of dense vegetation are calculated. To retrieve the equivalent parameters, a root-mean-square minimization technique is used. First of all, the brightness temperature was simulated by the Tor Vergata university model in the following situations:

- Frequency: 1.4 GHz, 2.69 GHz, 6.92 GHz and 10.45 GHz.
- Observation Angle: 10°, 20°, 30°, 40° and 50° incident angle.
- Gravimetric soil moisture content: 0.05–0.35 m³/m³, intervals 0.05 m³/m³.
- Polarization: vertical and horizontal.
- Root mean square height: 0.5–1.5 cm of 0.5.
- Correlation length: 5–15 cm, intervals of 5.

Since, scattering albedo and optical depth are independent of soil moisture and roughness parameter, by simulating brightness temperature from the Tor Vergata model in different soil

moisture and roughness parameters and fitting our simulation to the τ - ω model, it is possible to calculate effective vegetation parameters. The least square method (8) was used to obtain equivalent scattering albedo and equivalent optical depth simultaneously. In this study we named them EVOD and ESA respectively.

$$MIN \sqrt{\sum_{i=1}^N [\epsilon_{TVU} - \epsilon_0]^2} \quad (8)$$

By this method, EVOD and ESA depend on polarization, incident angle and frequency. N is the number of available

roughness parameters (in this study $N=63$), ϵ_{TVU} is the simulated total emissivity (the ratio of the simulated brightness

and the ambient temperatures), and ϵ_0 is the τ - ω model given in Equation 7. Here thermal equilibrium assumption between soil and vegetation was considered. The fitted τ - ω model codes are not publicly available due to ethical concerns. They can be requested from the author at [so.talebi@gmail.com].

3. Results

The Tor Vergata model simulation has been validated several times using field data for wheat (Eom and Fung, 1984; Ferrazzoli et al. 1995; Ferrazzoli and Guerriero, 1996; Ferrazzoli et al. 2000; Ferrazzoli et al. 2002). Figure 1 shows measured TB from radiometer and simulated TB from Tor Vergata model (L band, 40° incident angle).

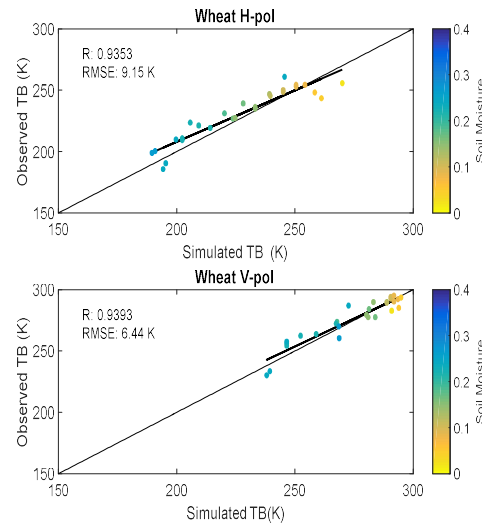


Figure 1. Comparison of radiometer measured and Tor Vergata model simulated of TB at L band in V and H pol (Talebiesfandarani et al. 2019).

It indicates the correlation coefficient between measured and simulated TB is 0.93 in V and H polarizations. The results provided an acceptable level of accuracy for the Tor Vergata model to be admitted as the theoretical basis for this study.

3.1 VODs retrievals from Tor Vergata University model:

Figure 2 indicated VODs simulation in L, S and C bands in two incident angles (10 and 50-degree) at V and H polarization. Canopy height added to the figure to compare.

The figure showed the VODs was frequency, incident angle and polarization dependent parameter. By increasing canopy

height VODs increased. VODs value at 50° incident angle was higher than 10° incident angle. VODs increased by frequency because this increase leads to the decrease of penetration depth. VODs at V polarization was higher than H polarization and more incident angle dependent. VODs at H polarization at L and S bands also are incident angle dependent but because of being the same y axis in all figures, it isn't clear enough.

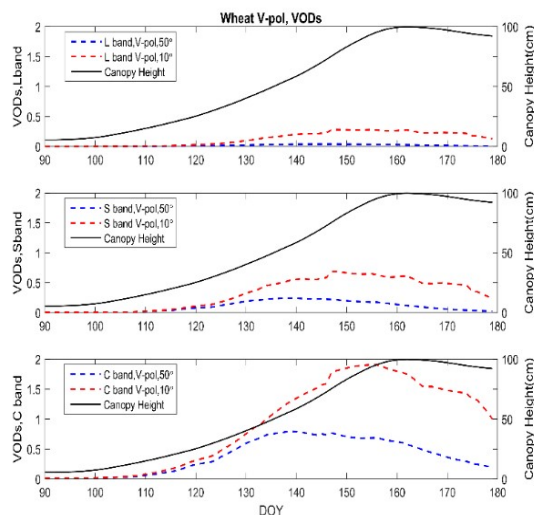


Figure 2. VODs simulation at V polarization in L, S and C bands and two incident angles (10 and 50 degree). When vegetation optical depth was calculated correctly, it can be as an indicator of vegetation growth. Here VODs was compared with measured LAI, VWC and biomass. Figure 3 indicated that VODs were corresponding to the measured vegetation parameters according to the trend and the time of maximum and the minimum values.

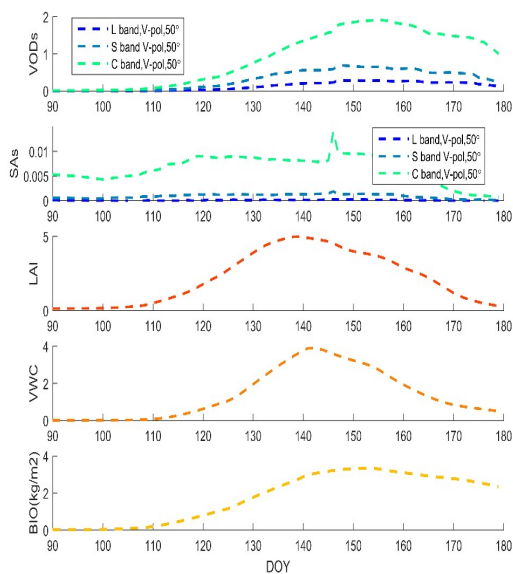


Figure 3. The trend of VODs compares to measured LAI, VWC and biomass for wheat

3.2 EVOD and ESA retrievals by fitted τ - ω model

Here, equivalent optical depth (EVOD) was calculated by fitting a high order model to zero order model to understand whether this way can work for a dense crop like wheat or not. To obtain equivalent optical depth, brightness temperature from TVU model was simulated and fitted with the τ - ω model. Figure 4 showed the EVOD for wheat at V polarization in three bands, L, S and C. Canopy height also added to the figure to compare.

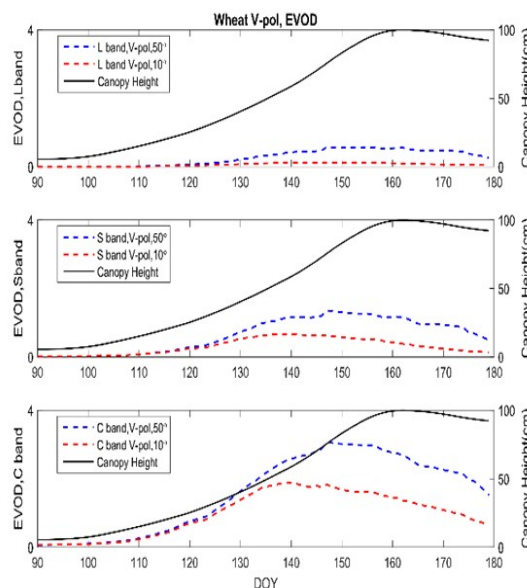


Figure 4. EVOD simulation at V and H polarization in L, S and C bands and two incident angles (10 and 50 degree). The figure indicated that increase in canopy height leads to increase in EVOD. EVOD value at 50° incident angle was higher than 10° incident angle. Another point that should be considered is that increasing EVOD by frequency. By increasing the frequency, penetration deep was decreased and optical depth was increased. Comparing EVOD with VODs (figure 2), it was indicated although the trends of EVOD and VODs in three bands were the same, but paying attention to the EVOD values indicated little overestimated compare to VODs. Comparing the EVOD with VODs is indicated that EVOD has acceptable correlation with VODs but is overestimated in L, S and C frequencies, H and V polarization and in 10- and 50-degree incident angles (figure 4). The smallest RMSE of the regression between VODs and EVOD occurs in L band. By increasing frequency, the RMSE increased.

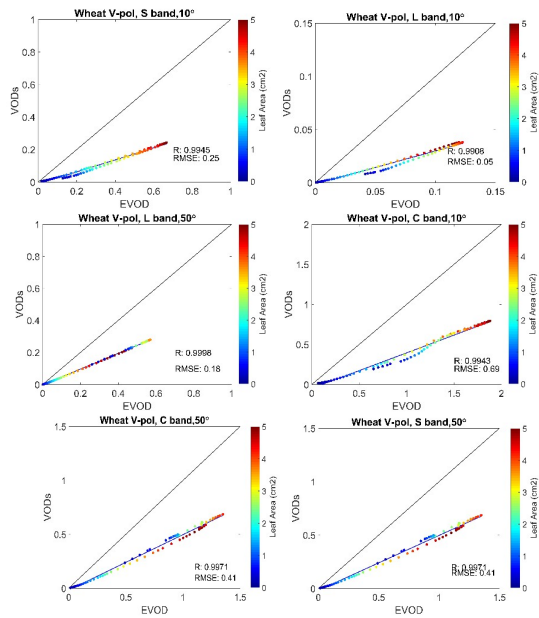


Figure 4. comparison of EVOD with VODs in L and S and C bands.

4. Discussion

The VODs was retrieved from Tor Vergata University model. The VODs depends on frequency, polarization and incident angle (Baur et al. 2019; Guangrui et al. 2021; Dou et al. 2023). By increasing canopy height, VODs increased because vegetation extinction was increased (Van de Griend and Wigneron, 2003; Hu et al. 2023; Liu et al. 2023). VODs value at 50° incident angle was higher than 10° incident angle (Wigneron et al. 2017). That's may because of longer observed vegetated canopy in 50° incident angle compare to in 10° incident angle. VODs was increased by frequency because of increasing penetration depth (Grant et al. 2016). Due to vertical structure of wheat, VODs at V polarization was higher than H polarization (Wigneron et al. 2004; Bai et al. 2018; Yao et al. 2024).

VODs was compared to the measured LAI, VWC and biomass. It was indicated that in V polarization, biomass and opacity had the best correlation with VOD (Schmidt et al. 2022).

Comparing the EVOD with VODs is indicated that lower frequencies are more suitable to calculate optical depth by fitted zero order model (like in SMAP and SMOS missions) (Schmidt et al. 2022). The least RMSE value derived for when L band in H and V polarization was applied.

Using equivalent optical depth derivation method in other types of vegetation with different structure can prepare more detail in potential of fitting method in dense vegetation.

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